

# On the Fairness-Efficiency Tradeoff for Packet Processing with Multiple Resources

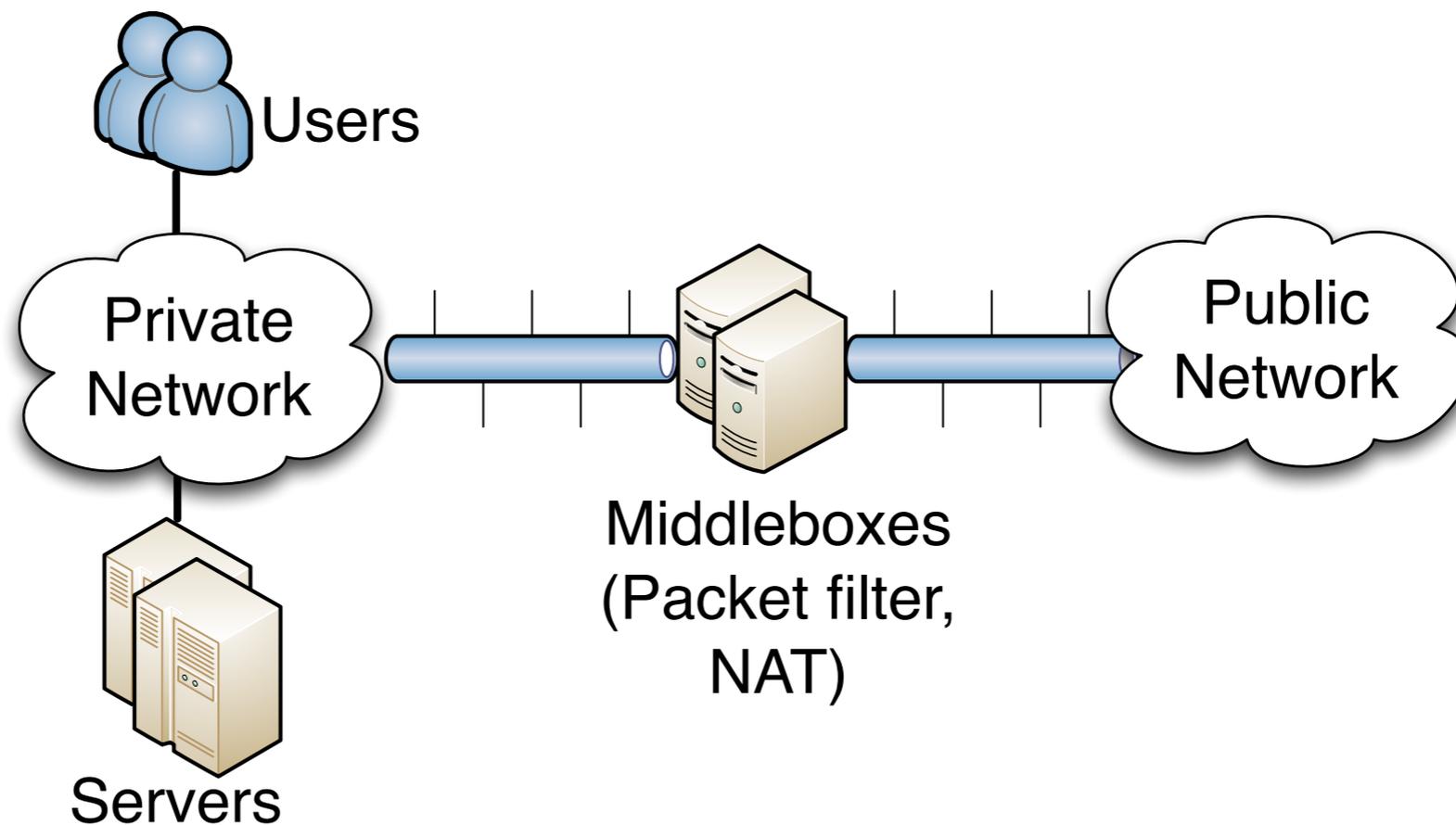
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# Middleboxes and Deep Packet Inspection

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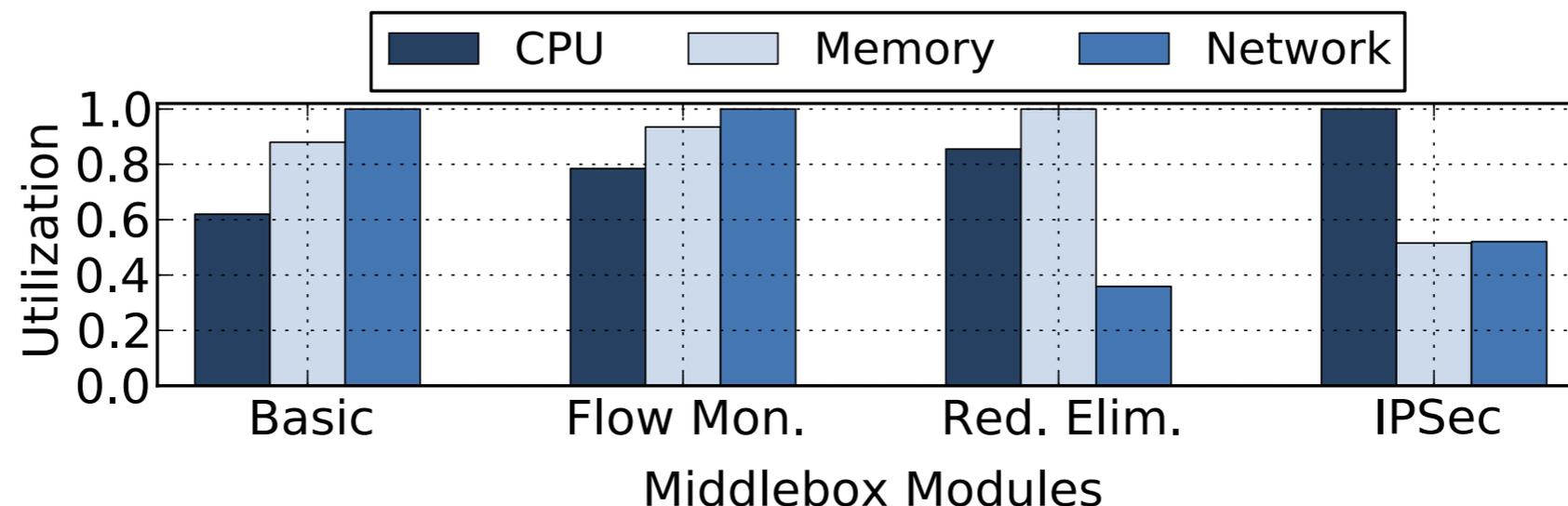
- ▶ Process packets based on payload
  - ▶ IPsec, Monitoring, Firewalls, WAN optimization, etc



# Consumption of Multiple Resources

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- ▶ Packet processing requires multiple types of resources (e.g., CPU, memory b/w, link b/w)
- ▶ Different middlebox (MB) modules consume different amounts of resources



Ghods et al. SIGCOMM'12

Resources should be shared **fairly**  
and **efficiently** among flows

# Fairness

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- ▶ Predictable service isolation
  - ▶ The service a flow receives in an  $n$ -flow system is at least  $1/n$  of that it achieves when the flow monopolizes all resources
- ▶ Dominant Resource Fairness (DRF)
  - ▶ Flows receive *approximately the same* processing time on the *dominant resources* of their packets

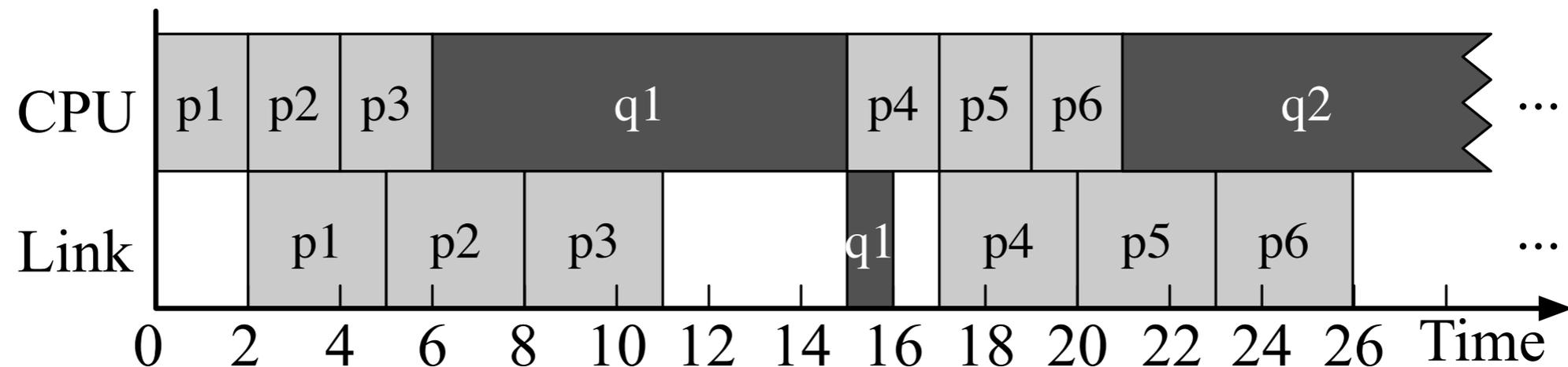
# Efficiency

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- ▶ High resource utilization given a non-empty system, with high traffic throughput
- ▶ Important in today's enterprise networks, as a surging volume of traffic now passes through MBs

However, fairness and efficiency are **conflicting** objectives in the presence of multiple resources

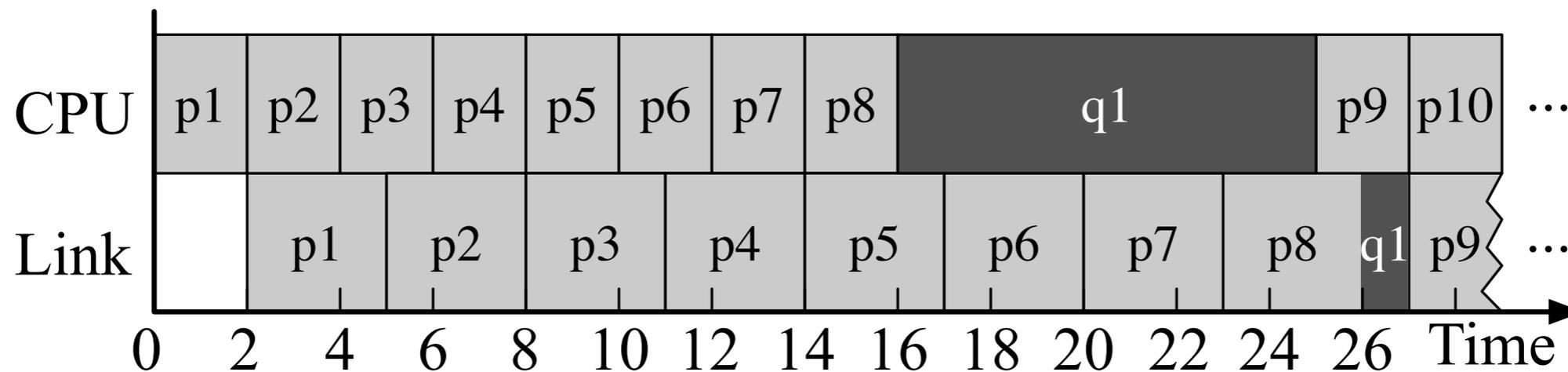
# Fair but Inefficient



(a) A packet schedule that is fair but inefficient.

- ▶ Fair: both flows receive 9 time units to process on their dominant resources in each round
- ▶ Inefficient: link is idle at 1/3 of time

# Efficient but Unfair



(b) A packet schedule that is efficient but unfair.

- ▶ Unfair: Flow 1 receives 96% of the link bandwidth; Flow 2 receives 36% of the CPU time
- ▶ Efficient: 100% CPU and link utilization given a non-empty system

# Ideally...

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- ▶ Allow the network operator to flexibly specify the tradeoff preference
  - ▶ Many applications may have loose fairness requirements
- ▶ Implement the specified tradeoff via a queueing algorithm

# However...

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- ▶ Existing multi-resource queueing algorithms focus only on fairness, without efficiency consideration
  - ▶ The tradeoff problem has never been mentioned before, and is **unique** to multi-resource scheduling
- ▶ Even the efficiency measure is unclear!

# The Efficiency Measure

# Schedule Makespan

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- ▶ Time elapsed from the arrival of the first packet to the time when all packets finish processing on all resources
  - ▶ The completion time of the last flow

Max efficiency = Min makespan

# Quantifying the Efficiency Loss

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- ▶ Theoretical results
  - ▶  $m$ : # of resource types concerned
  - ▶ the makespan of fair queueing could be up to  $m$  times the optimal makespan
- ▶ Experiment confirms 20% throughput loss of existing multi-resource fair queueing

Makespan minimization is notoriously hard, especially when there are more than two types of resources concerned (NP-hard)

We limit our discussion to the two most concerned types of resources for packet processing—CPU and link bandwidth

# Our Approach

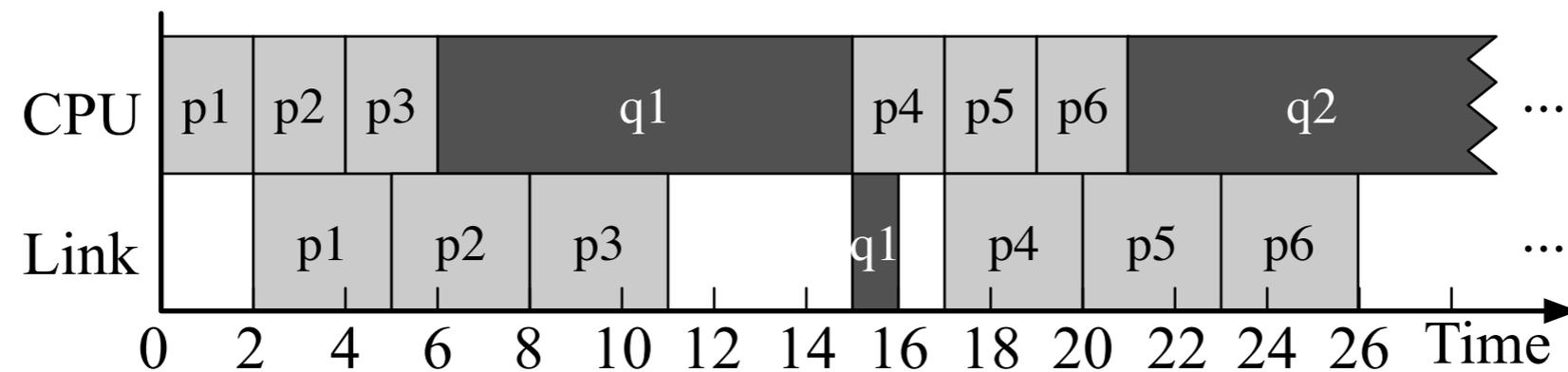
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- ▶ Relax the scheduling problem to an idealized *fluid model*
- ▶ Discuss the tradeoff between fairness and efficiency in the fluid model
- ▶ Implement the fluid model in the real world via a packet-by-packet tracking algorithm

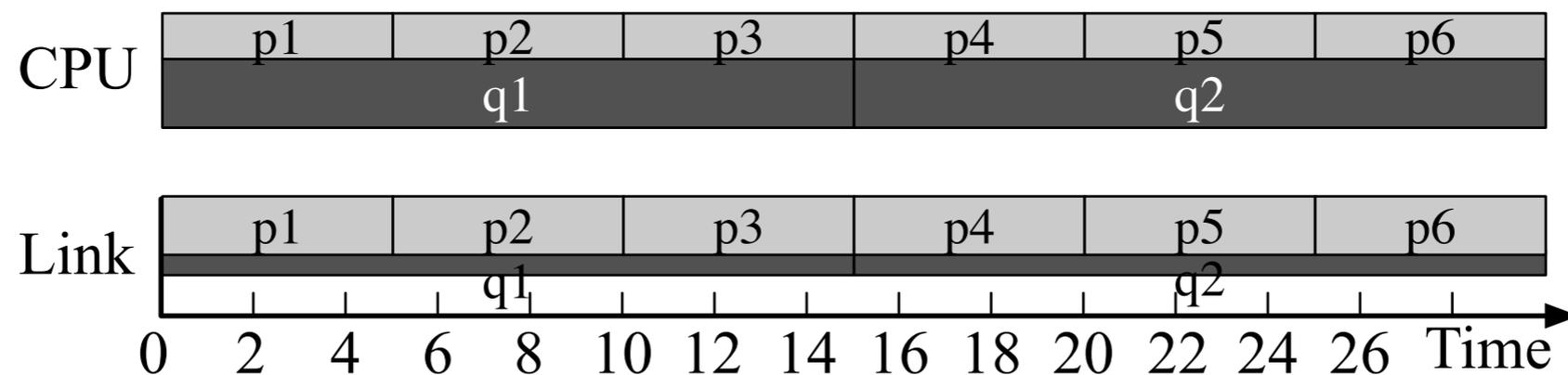
**The Fluid Relaxation:** packets are assumed to receive services in arbitrarily small increments on all resources

# Fluid Relaxation

- ▶ Discrete schedule



- ▶ Fluid relaxation



# Fluid w/ the Perfect Fairness

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- ▶ Implement the strict DRF allocation at all times

Max-min flow's dominant share

$$\begin{aligned} \max_{d_i} \quad & \min_{i \in \mathcal{B}} d_i \\ \text{s.t.} \quad & \sum_{i \in \mathcal{B}} \bar{\tau}_{i,r} d_i \leq 1, \quad r = 1, 2. \end{aligned}$$

Resource constraints

- ▶ All flows receive the same *fair dominant share*

$$\bar{d} = 1 / \max \left\{ \sum_i \bar{\tau}_{i,1}, \sum_i \bar{\tau}_{i,2} \right\}$$

# Fluid w/ the Optimal Efficiency

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- ▶ Greedily maximizes the *system dominant share* at all times

Maximize system dominant share

$$\begin{array}{ll} \max_{d_i \geq 0} & \sum_{i \in \mathcal{B}_t} d_i \\ \text{s.t.} & \sum_{i \in \mathcal{B}_t} \bar{\tau}_{i,r} d_i \leq 1, \quad r = 1, 2. \end{array}$$

Resource constraints

# Fairness-Efficiency Tradeoff

# Specifying Fairness Requirement

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- ▶ Let  $\bar{d}$  be the *fair dominant share* under DRF
- ▶ Let  $\alpha \in [0, 1]$  be a *fairness knob* specified by the operator
- ▶ **Fairness constraint:** flows receive at least  $\alpha$ -portion of fair dominant share

$$d_i \geq \alpha \bar{d}, \quad \forall i \in \mathcal{B},$$

Fair share under DRF

Dominant share of flow  $i$

# Fairness-Efficiency Tradeoffs

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- ▶ Maximize the *system dominant share* under a specified tradeoff level (quantified by fairness knob  $\alpha \in [0, 1]$ )

$$\begin{aligned} \max_{d_i} \quad & \sum_{i \in \mathcal{B}_t} d_i && \text{Resource constraint} \\ \text{s.t.} \quad & \sum_{i \in \mathcal{B}_t} \bar{\tau}_{i,r} d_i \leq 1, \quad r = 1, 2, \\ & d_i \geq \alpha \bar{d}, \quad \forall i \in \mathcal{B}_t . \end{aligned}$$

Fairness constraint

Implement the fluid model via  
packet-by-packet tracking

# Start-Time Tracking

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- ▶ Maintain the Tradeoff Fluid as a reference system in the background
- ▶ In the real world, whenever there is a packet scheduling opportunity, the one that starts the **earliest** in the Tradeoff Fluid is scheduled first
- ▶ An  $O(\log n)$  implementation based on a *special structure* of the Tradeoff Fluid
- ▶ **Asymptotically close** to the fluid model in terms of both makespan and fairness guarantee

# Evaluation

# Experiment Setup

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- ▶ Prototype implementation in Click modular router
- ▶ 60 UDP flows each sending 2,000 800-byte pkts/s
- ▶ Three middlebox processing modules
  - ▶ Packet checking (bandwidth-bound): Flows 1~20
  - ▶ Statistical monitoring (bandwidth-bound): Flow 21~40
  - ▶ IPsec (CPU-bound): Flows 41~60

Scenario 1: No packet drop

# Makespan

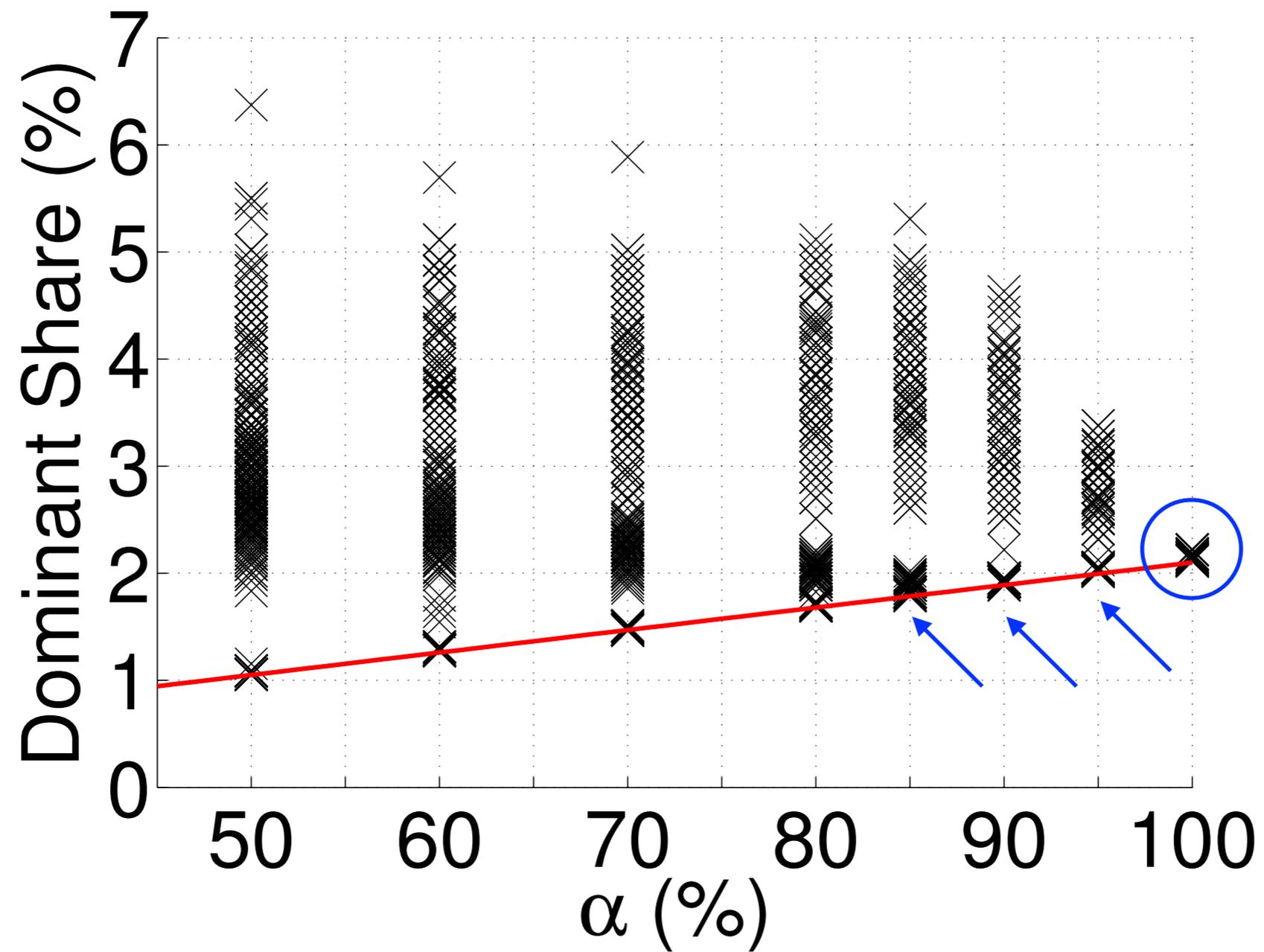
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- ▶ Each flow sends 10s traffic

$\alpha$	<b>Makespan (s)</b>	<b>Normalized Makespan (%)</b>
1.00	55.68	100.00
0.95	52.50	94.28
0.90	48.97	87.95
0.85	47.17	84.72
0.70	47.13	84.64
0.60	47.07	84.54
0.50	47.07	84.54

- ▶ Trading off 15% of fairness is sufficient to achieve the shortest makespan (20% throughput improvement)

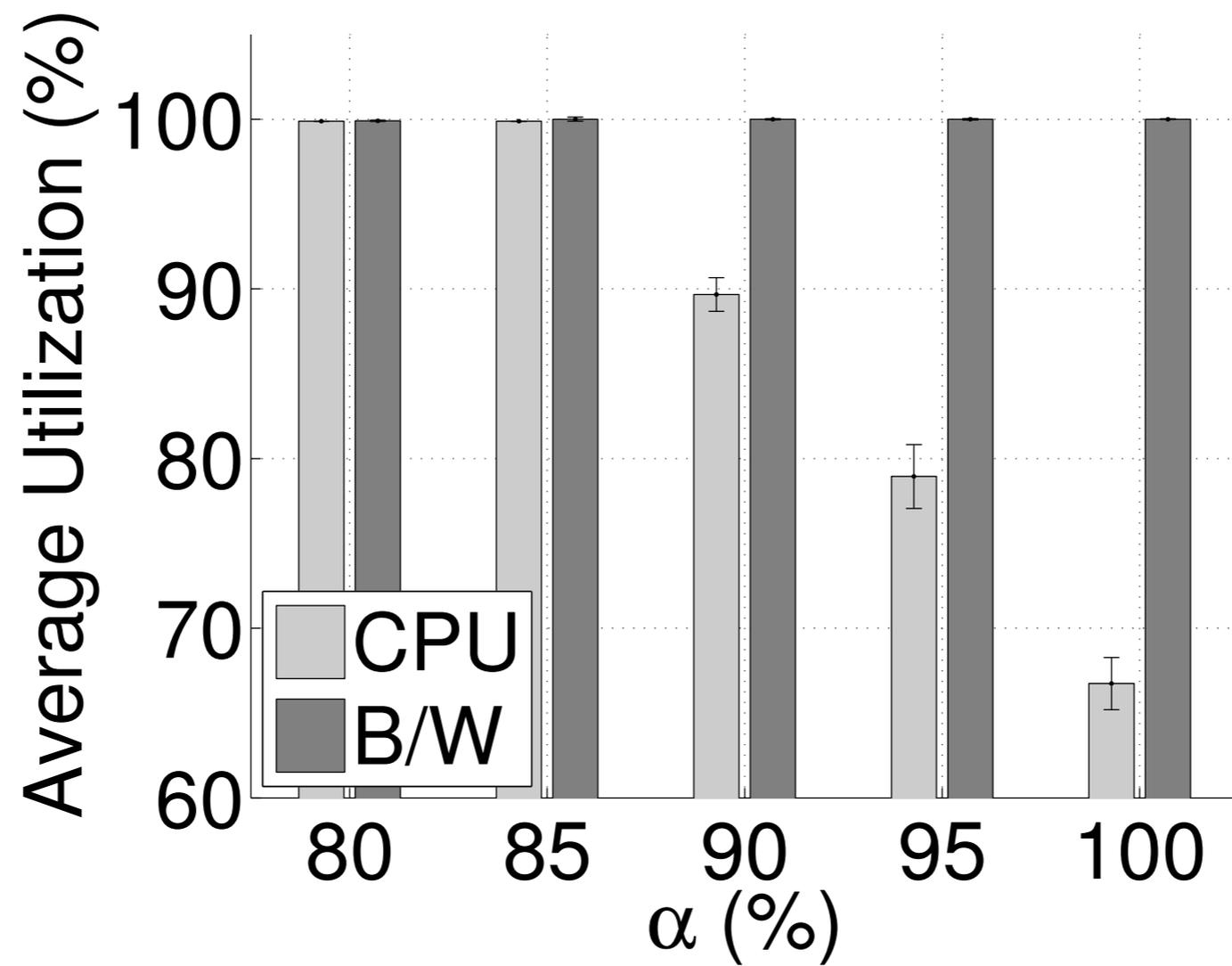
# Fairness



Scenario 2: buffer size=200

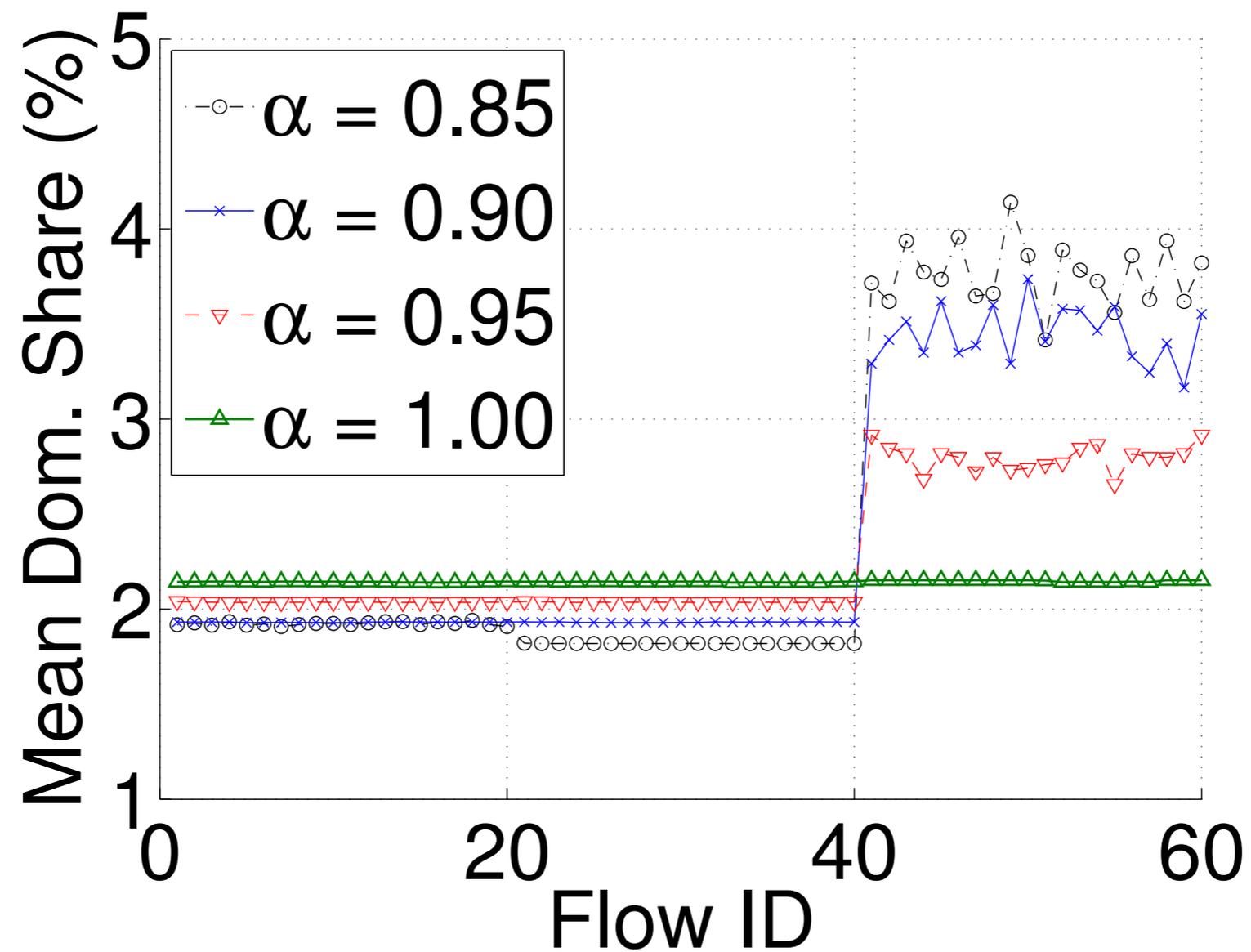
# Resource Utilization

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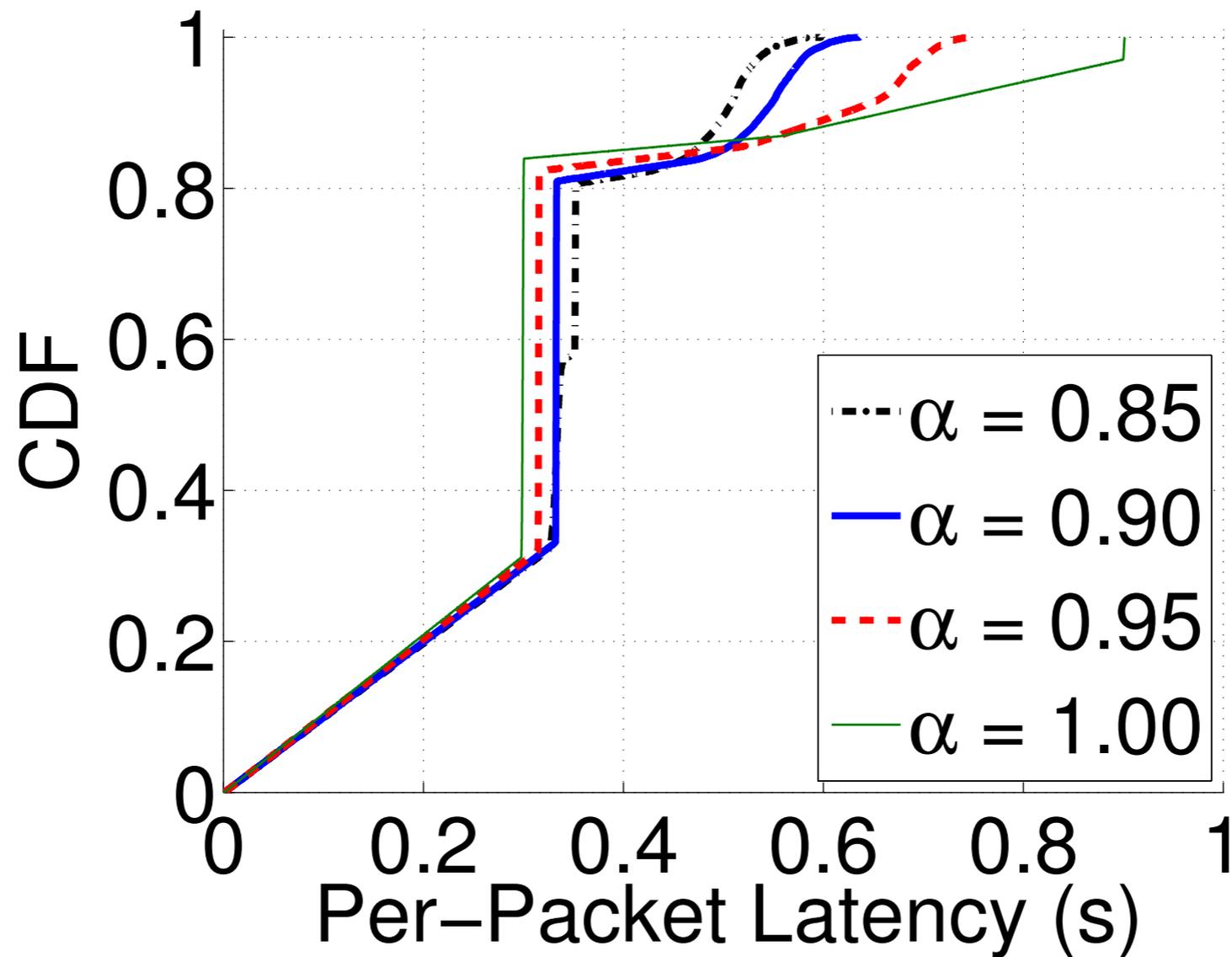
# Dominant Share

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# Per-Packet Latency

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# Conclusions

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- ▶ We have identified the problem of fairness-efficiency tradeoffs for multi-resource packet scheduling
- ▶ We have designed a scheduling algorithm to achieve a flexible tradeoff between fairness and efficiency for packet processing that requires both CPU and link bandwidth
- ▶ We have prototyped the tradeoff algorithm in Click. Experimental results show that slight fairness tradeoff is sufficient to achieve the highest efficiency

# Thank you!

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