$$f_0 = \frac{\lg \pi}{2} - \frac{1}{2 \log 2} - \frac{1}{4}$$