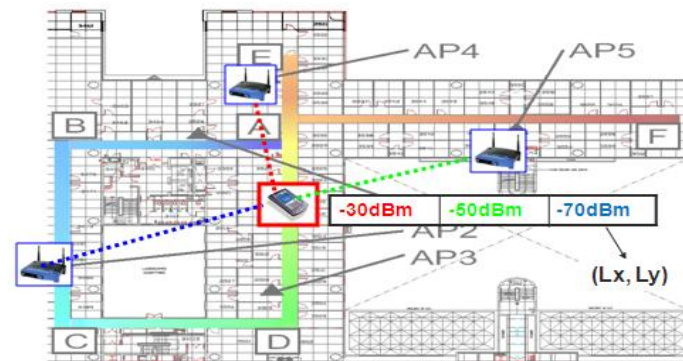


# Transferring Localization Models Over Time

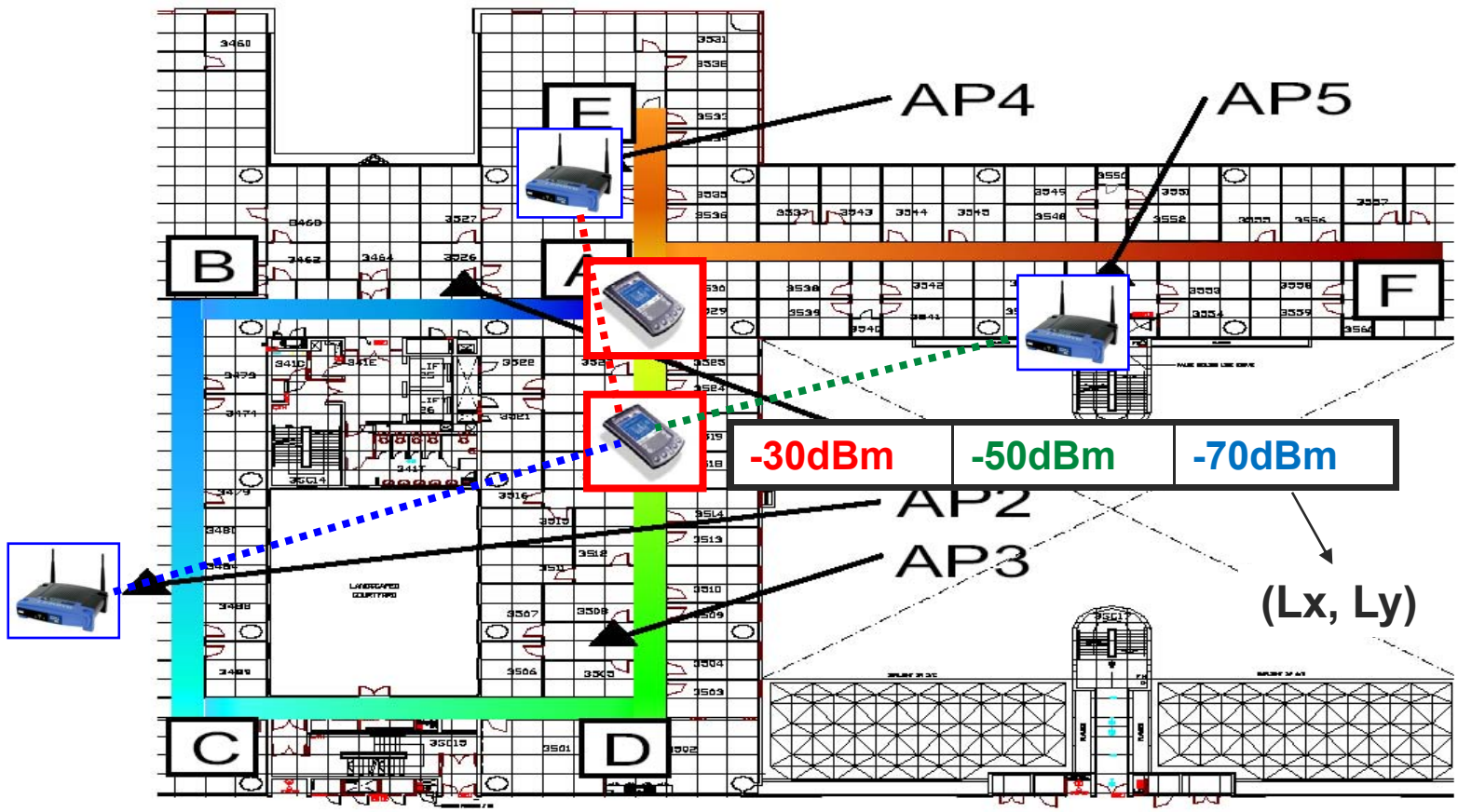
Vincent W. Zheng, Evan W. Xiang, Qiang Yang, Dou Shen  
Department of Computer Science and Engineering  
Hong Kong University of Science and Technology

Present in the 23rd AAAI Conference  
on Artificial Intelligence (AAAI-08).  
Chicago, Illinois, USA. July 2008.

<http://www.cse.ust.hk/~vincentz>



# Signal-strength-based Localization



# Learning-based Location Estimation

- Two phases: **training** and **localization**
- **Training phase** – collect a set of signal-location pairs and learn a mapping function

(AP1, AP2, AP3)	(Lx, Ly)
( -30, -50, -70 ) dBm	( 2, 7 ) m
( -40, -45, -75 ) dBm	( 3, 11 ) m
.....	...

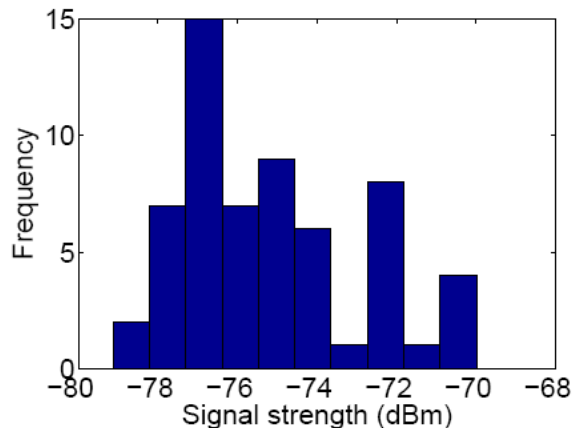


Mapping function  
from signal to location  
 $F : S \rightarrow L$

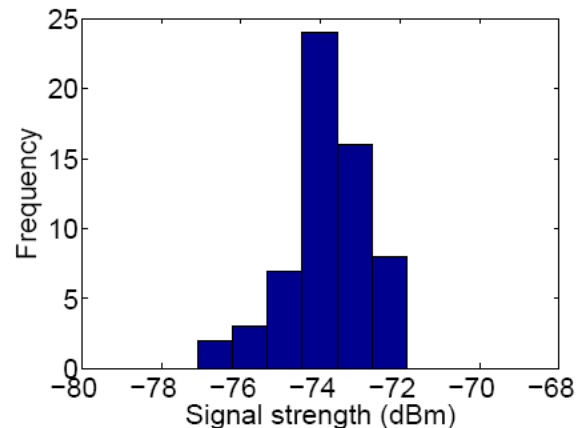
- **Localization phase** – given a signal **S**, predict its most probable location  $L = F(S)$

# Our focus: signal variation over time

- Traditional localization methods assume:
  - Training and testing data have **same** distributions
  - Do not address whether localization model is **out-of-date**
- However, in practice,
  - **Different** time periods, **different** signal distributions



(a) WiFi signal at time period 1



(b) WiFi signal at time period 2

# Related works

- Only some work address the signal variation over time

Algorithm	Basic idea	Con's
RADAR (Bahl <i>et al.</i> 2000)	KNN	Do not consider signal variation.
LANDMARC (Ni <i>et al.</i> 2003)	Weighted-KNN	Require a large amount of hardwares.
ModelTree (Yin <i>et al.</i> 2005)	Regression analysis and decision tree	Do not use the user trace information.
LeManCoR (Pan <i>et al.</i> 2007)	Manifold co-regularization	Do not use the user trace information.

# Transferring Localization Models over Time

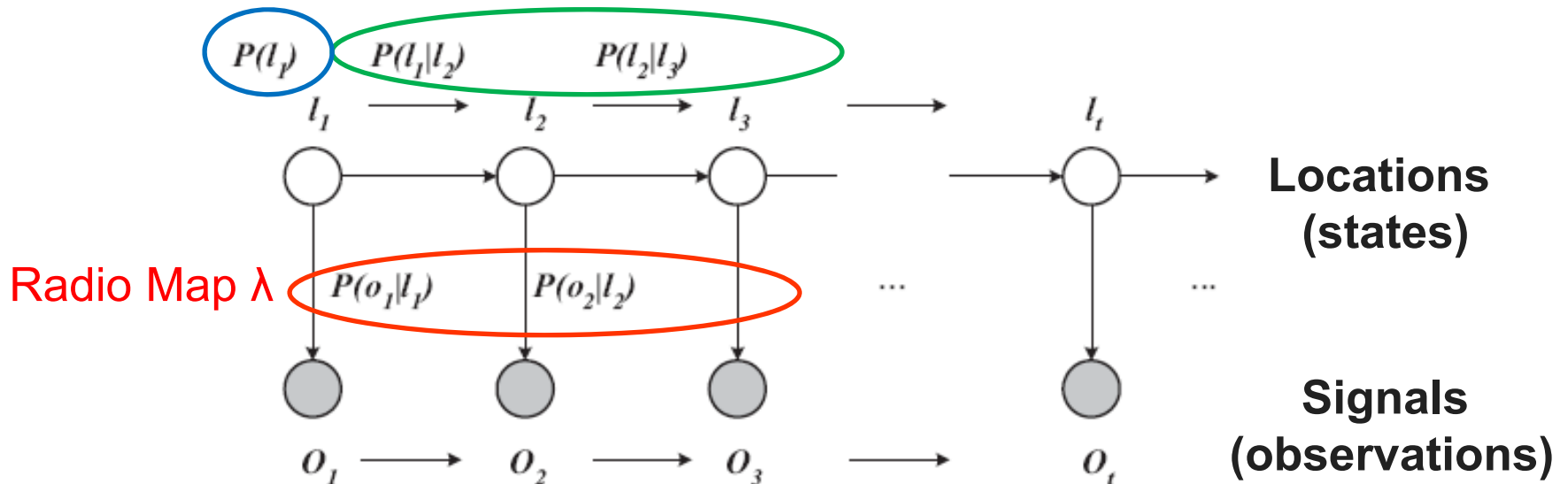
- The Question:
  - Given some labeled **out-of-date data**, how to use as few **up-to-date labeled/unlabeled data** as possible to calibrate the localization model?
- Our Solution: Transferred HMM (TrHMM)
  - Exploit the HMM for localization
  - **What to transfer?** – uncover which parts of the model knowledge can be **reused**, and which parts need to be **adapted** by up-to-date information
  - **How to transfer?** – A domain-specific solution for HMM model transfer

# Our Solution: Transferred Hidden Markov Model

- Hidden Markov Model –  $\theta = (\lambda, A, \pi)$

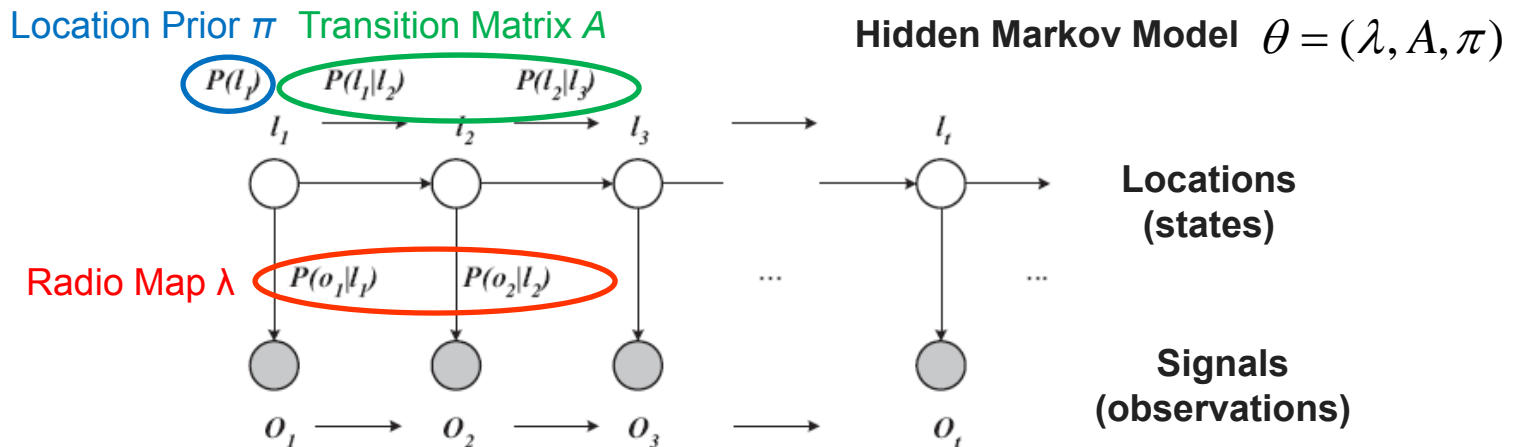
Location Prior  $\pi$

Transition Matrix  $A$



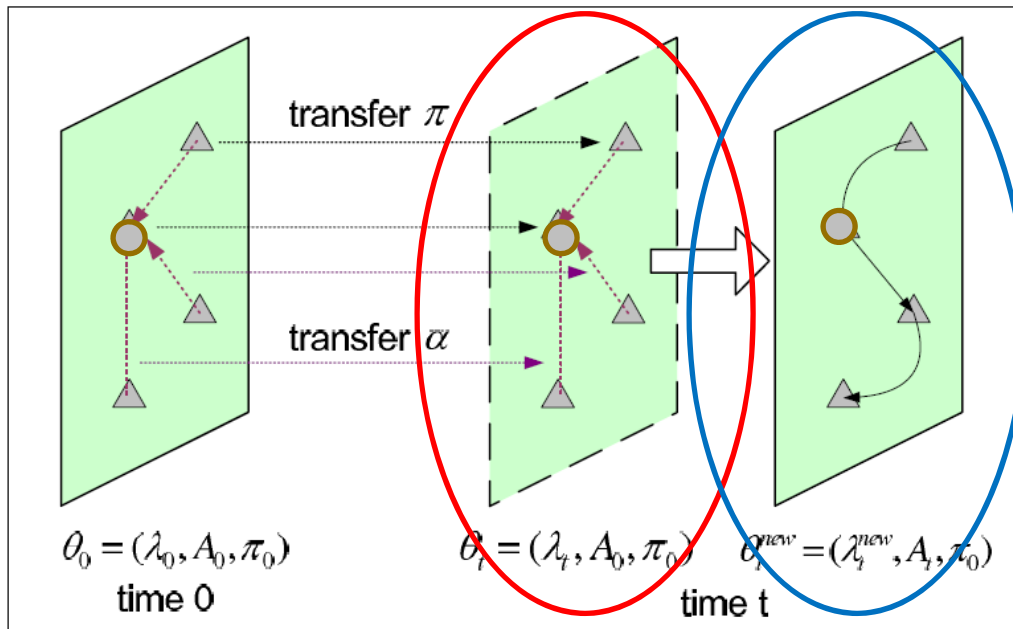
# Our Solution: Transferred Hidden Markov Model (Cont')

- What to transfer?
  - $\lambda$  changes, due to signal variation over time
  - $A$  changes, since behaviors are different at different time
  - $\pi$  keep unchanged, since basic behaviors does not vary much



# Our Solution: Transferred Hidden Markov Model (Cont')

## How to transfer?



### Update radio map:

- (1) Employ **reference points\*** to collect up-to-date signals;
- (2) Apply **regression analysis** to fit the signals on non-reference points.

### Update transition matrix & radio map:

- (1) Collect **unlabeled traces**;
- (2) Expectation maximization (**EM**) to update the model.

\* Reference points are the hardware installed in the environment to continuously collect signals.

# Our Solution: Transferred Hidden Markov Model (Cont')

## ■ Update the radio map

- Step 1 – at time 0, for each AP  $j$ , fit the (signal) **regression model**  $\alpha$  among reference points and non-reference point  $k$

$$s_j^k = \alpha_{0j}^k + \alpha_{1j}^k r_{1j} + \dots + \alpha_{nj}^k r_{nj} + \varepsilon_j$$

where,  $r_{ij}$  is the signal at reference point  $i$  ( $i=1, \dots, n$ ).

- Step 2 – at time  $t$ , collect up-to-date signals on reference points, and use  $\alpha$  to **predict** signals on non-reference points;
- Step 3 – **update** the radio map by **trading off** predicted value with the base radio map

$$\mu_t = \beta \cdot \mu_0 + (1 - \beta) \cdot \mu_t^{reg}$$

$$\Sigma_t = \beta \cdot \left[ \Sigma_0 + (\mu_t - \mu_0)(\mu_t - \mu_0)^T \right] + (1 - \beta) \cdot \left[ \Sigma_t^{reg} + (\mu_t - \mu_t^{reg})(\mu_t - \mu_t^{reg})^T \right]$$

# Our Solution: Transferred Hidden Markov Model (Cont')

- Update the transition matrix & radio map

- Step 1 – collect up-to-date unlabeled traces  $T=\{tr_i\}$
- Step 2 – expectation maximization to update model

- E-step:

$$P(q | tr, \theta^k) = \frac{P(tr, q | \theta^k)}{P(tr | \theta^k)} = \frac{P(tr | q, \theta^k) P(q | \theta^k)}{\sum_q P(tr | q, \theta^k) P(q | \theta^k)}$$

where,  $P(tr | q, \theta^k) = \prod_{n=1}^{|tr|} P(\mathbf{o}^n | l^n, \theta^k) \dots \lambda$

$$P(q | \theta^k) = P(l^1 | \theta^k) \times \prod_{n=1}^{|tr|} P(l^n | l^{n-1}, \theta^k) \dots \pi + A$$

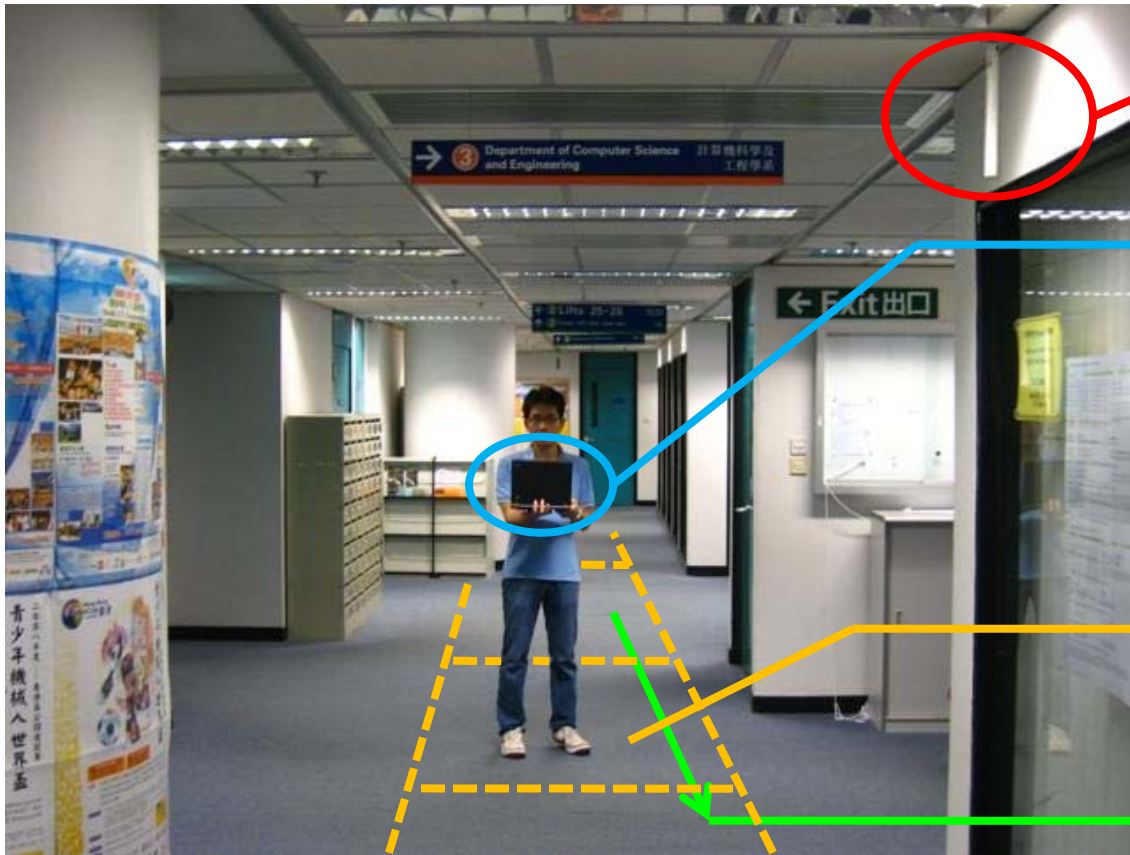
- M-step:

$$\theta^{k+1} = \arg \max_{\theta} Q(\theta, \theta^k) = \arg \max_{\theta} \sum_{tr \in T} \sum_q P(q | tr, \theta^k) \log P(tr, q | \theta)$$

# The Algorithm for TrHMM

- **Input:** Labeled data at time 0, labeled data from reference points and unlabeled traces at time  $t$ , test traces at time  $t$
- **Output:** labels for test traces
- Training phase
  - Time 0 – build the base Hidden Markov Model  $\theta_0$
  - Time  $t$  – update the base model to  $\theta_t$ 
    - update the **radio map  $\lambda$**  – regression analysis by using reference points data
    - update the **transition matrix  $A$**  – EM by using unlabeled traces data
- Localization phase
  - **Predict** the labels for test traces by using updated model  $\theta_t$

# [ Experimental Setup ]



WiFi Access Point (AP)

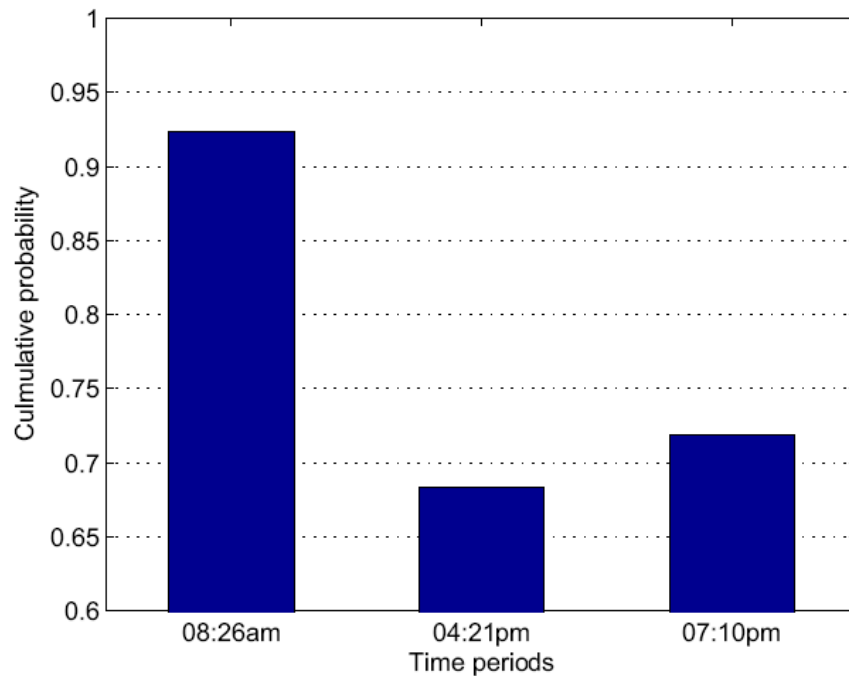
Collect WiFi signals

Academic building  
64 x 50 m<sup>2</sup>,  
discretized into 118  
1.5x1.5 m<sup>2</sup> grids.  
Each grid = a reference point

User moves in the building

# Experimental Results

- Necessity for considering time-variation problem



**Time 0:**  
08:26am

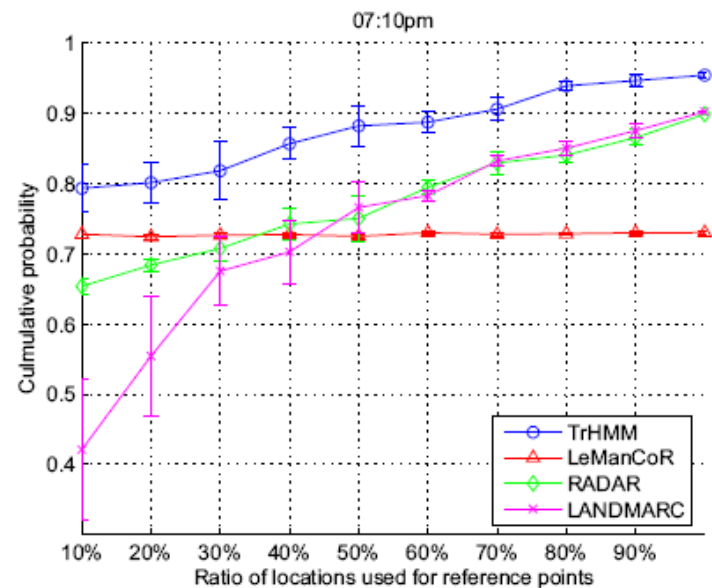
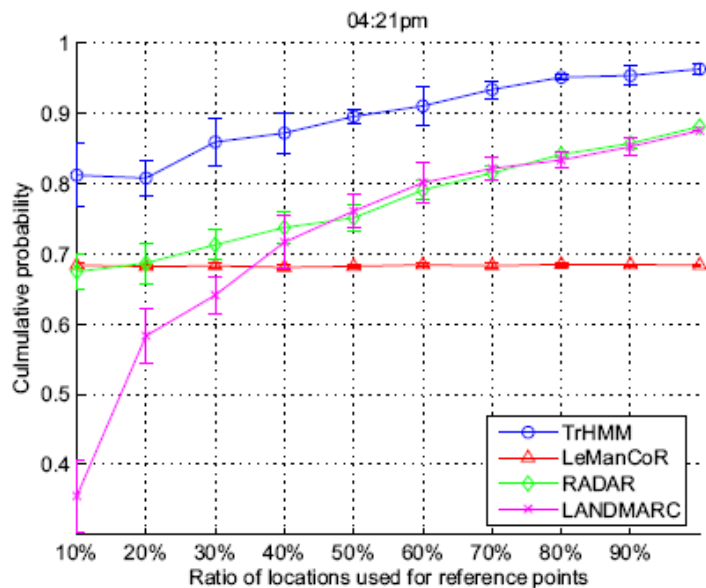
**Time t:**  
04:21pm & 07:10pm

**Measurement:**  
prediction accuracy\*  
(with 3-meter error distance)

\* The *higher*, the *better*.

# Experimental Results (Cont')

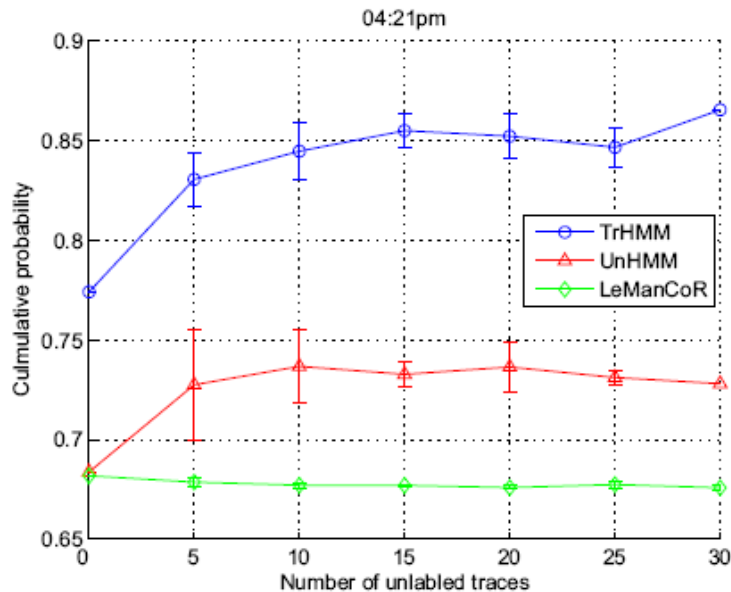
## Impact of reference points (labeled data)



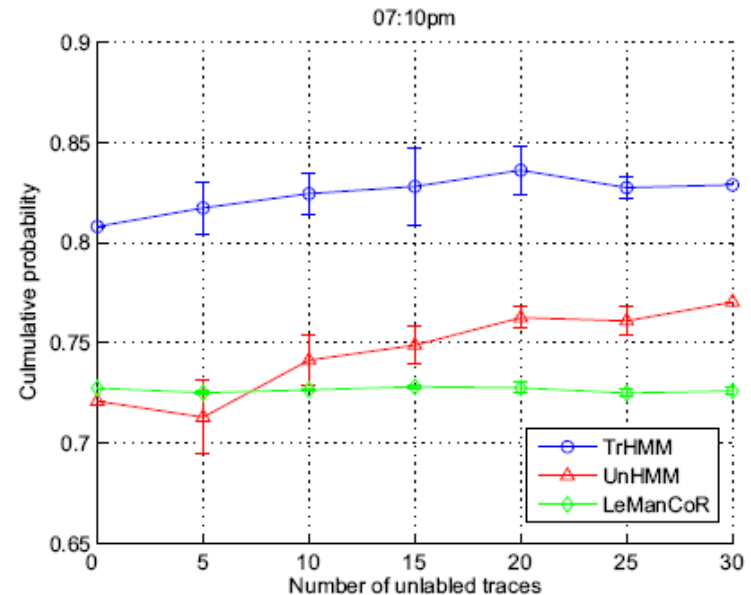
(a) Impact of reference points for 04:21pm (b) Impact of reference points for 07:10pm

# Experimental Results (Cont')

## Impact of unlabeled traces (unlabeled data)



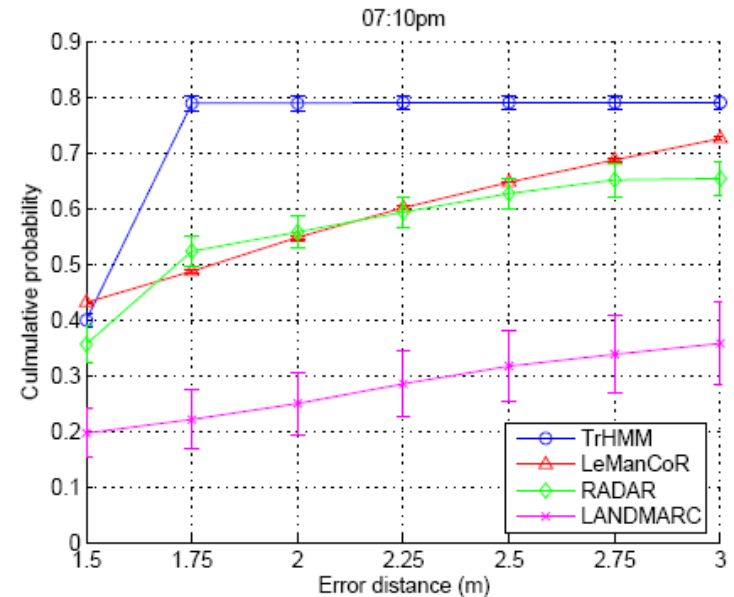
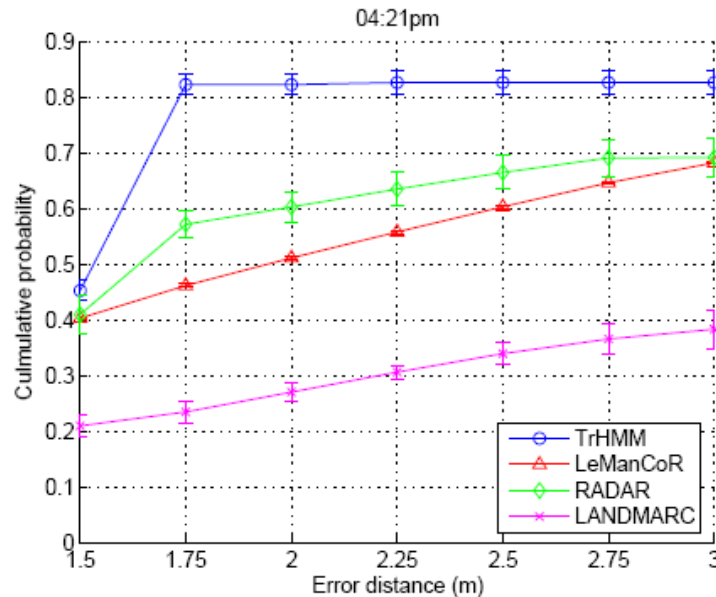
(c) Impact of unlabeled data for 04:21pm



(d) Impact of unlabeled data for 07:10pm

# Experimental Results (Cont')

## Sensitivity to error distance



(e) Sensitivity to error distance for 04:21pm (f) Sensitivity to error distance for 07:10pm

# Conclusion and Future Work

## ■ The Algorithm

## Conclusion

- Signal variation over time
- Transferred Hidden Markov Model
- Utilize the out-of-date data to help update model
- Regression analysis and EM optimization

## ■ Algorithm level

## Future Work

- Extend to online setting
- Exploit how to optimally select subset of labeled data

## ■ Application level

- Incorporate transfer learning with Gaussian Process (*Ferris, Fox, & Lawrence 2007*) for localization

[ The End ]

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**Thank You !**  
**Welcome to our poster  
presentation!**  
Questions?