

DSAA 5012: Database Management Systems in Data Science

Lecture 9 Exercises Functional Dependencies 1: Introduction

Exercise 1: Assume that this table contains the *only* set of tuples that may appear in a relation $R(X, Y, V, W)$. Which of the following FDs hold in R ?

- $X \rightarrow X$ Yes No $Y \rightarrow X$ Yes No
 $X \rightarrow Y$ Yes No $W \rightarrow X$ Yes No
 $X \rightarrow V$ Yes No $XV \rightarrow Y$ Yes No
 $X \rightarrow W$ Yes No $YV \rightarrow X$ Yes No

tuple	X	Y	V	W
1	x ₁	y ₁	v ₁	w ₁
2	x ₁	y ₁	v ₂	w ₂
3	x ₂	y ₁	v ₁	w ₃
4	x ₂	y ₁	v ₃	w ₄

Exercise 2: In Exercise 1, we assumed that we know all possible records in the table, which is not usually true. In general, by looking at an instance of a relation, we can only tell FDs that are not satisfied. List 5 FDs that are not satisfied in the table.

A	B	C
a ₁	b ₁	c ₁
a ₁	b ₁	c ₂
a ₂	b ₁	c ₁
a ₂	b ₁	c ₃

Exercise 3: Given relation schema $R(X, Y, U, V, W)$ and $F = \{X \rightarrow Y, UV \rightarrow W, V \rightarrow X\}$

a) Determine the closure of each attribute.

$X^+ =$ $U^+ =$ $W^+ =$
 $Y^+ =$ $V^+ =$

b) What are the candidate keys of R ?

Exercise 4: Given relation schema $R(A, B, C, G, H, I)$ and $F = \{A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H\}$

a) Is AG a (super)key of R given F ?

b) Is AG a candidate key?

c) Does $A^+ \rightarrow R$ hold?

d) Does $G^+ \rightarrow R$ hold?

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Exercise 5: Given relation schema $R(A, B, C, D, E)$ and $F = \{A \rightarrow B, AB \rightarrow C, D \rightarrow AC\}$

a) Determine the following attribute closures.

$A^+ =$

$C^+ =$

$E^+ =$

$B^+ =$

$D^+ =$

b) What are the candidate keys of R ?

c) Find a canonical cover of F .

Exercise 6: We want to create the database for a bank that contains accounts (A), branches (B) and customers (C). We are given the following constraints.

- i. An account cannot be shared by multiple customers.
- ii. Two different branches do not have the same account.
- iii. Each customer can have at most one account in a branch (but different accounts in different branches).

a) What are the functional dependencies implied by the above constraints?

b) What are the candidate keys?

Exercise 7: Given relation schema $R(A, B, C)$. Assume we do not know the keys of the relation. Write a valid SQL query whose result can be used to determine if A is a potential candidate key. Explain how to interpret the query result to determine if A is a potential candidate key.